## Applications

Anything that we can do to raise personal savings is very much in the interest of this country.
-Alan Greenspan, economist

1. How might those words apply to what has been outlined in this section? What "play on words" do you notice in Greenspan's quote? See margin.
2. The sixth-grade class at West Side School starts a charity collection on Monday, with $\$ 78$ donated by the Parents Organization. They plan to add $\$ 2$ to the fund each day. How much will they have after 90 days? $\$ 256$
3. Arrange the following interest rates in ascending order: $3.4 \%, 3.039 \%, 3 \frac{3}{16} \%$, $3.499 \%, 3 \frac{1}{2} \% .3 .039 \%, 3 \frac{3}{16} \%, 3.4 \%, 3.499 \%, 3 \frac{1}{2} \%$
4. A finite arithmetic sequence has 12 terms. The last term is 100 and the common difference is 3 . What is the first term? 67
5. Josh has a savings account at a bank that charges a $\$ 10$ fee and pays no interest for every month his balance falls below $\$ 1,000$. His account has a balance of $\$ 1,203.44$ and he withdraws $\$ 300$. What will his balance be in 6 months if he makes no deposits or withdrawals? \$843.44
6. Linda's savings account balance has fallen below the $\$ 1,000$ minimum balance required to receive interest. It is currently $\$ 871.43$. The monthly fee charged by the bank for falling below the minimum is $x$ dollars. Express algebraically how you compute the number of months it will take Linda's account to reach a zero balance if she makes no deposits. Explain. If $x=9$, how many months will it take? See margin.
7. John, Paul, and George are having a disagreement over interest rates. John says that $63 / 4 \%$ can be expressed as $6.75 \%$. George thinks that $63 / 4 \%$ can be expressed as 0.0675 . Paul remembers converting percents to equivalent decimals and thinks it can be expressed as $0.0675 \%$. Who is correct, and who is incorrect? Explain. See margin.
8. Beth and Mark would like to put some savings in the bank. They most likely will not need this money for 4 years, so Beth wants to put it in a 4 -year CD. Mark wants to put the money in a savings account. What is the advantage of a CD ? What is the disadvantage? See margin.
9. Find the simple interest on a $\$ 2,350$ principal deposited for 6 years at a rate of $2.77 \%$. $\$ 390.57$
10. Ryan deposits $\$ 775$ in an account that pays $1.24 \%$ simple interest for 4 years. Brian deposits $\$ 775$ in an account that pays $1.24 \%$ simple interest for 1 year.
a. What is Ryan's interest after the 4 years? $\$ 38.44$
b. What is Ryan's balance after 4 years? $\$ 813.44$
c. How much interest did Ryan's account earn the first year? \$9.61
d. How much interest did Ryan's account earn the fourth year? $\$ 9.61$
e. What is Brian's interest after the first year? \$9.61
f. What is Brian's balance after the first year? $\$ 784.61$
g. Suppose Brian withdraws all of the principal and interest after the first year and deposits it into another 1 -year account at the same rate. What is his interest for the second year? Round to the nearest cent. \$9.73
h. Compare the interest Brian earns with the interest Ryan earns for the second year. Who earned more interest? Explain. Brian earned more since he got interest on his first year's interest during the second year.

## TEACH

## Exercise 3

When students need to convert percents to fractions, have them convert the fractional part to a decimal first, and then move the decimal point.

## Exercise 5

Point out that this account pays no interest when the balance falls below the minimum.

## Exercise 10

This exercise plants the seeds for the underlying concept of compound interest, which is in the next lesson. Notice that if Brian redeposits his principal and interest each year, he is compounding his interest.

## ANSWERS

1. In addition to the pun on "interest," Greenspan thinks that savings help in several ways. They provide citizens with a financial cushion. They also give banks more money to lend for people to buy homes, cars, and so on.
2. $\frac{871.43}{x} ; 97$ months. Although the quotient is around 96.825 , it is not until the 97th month that the balance will reach zero.
3. John and George are correct. Paul is incorrect - when the percent is changed to an equivalent decimal, the percent sign is dropped.
4. The advantage of the $C D$ is a higher rate of interest. The disadvantage is that the CD has a penalty if the money is withdrawn before maturity and the money is not available for withdrawals.

## TEACH

Exercise 11
Remind students that if the number of months is not a counting number, they need to round up. Also, if they get a fraction of a year they can multiply by 12 to get the number of months.

## Exercises 17 and 21

Remind students that if they have trouble with formulating literal algebraic expressions, they can solve the same problem with numbers first to see how the variables should be manipulated.

## Exercises 18 and 19

Point out that there are no deposits made to these accounts, and that might be unrealistic. Tell them they learn how to handle long-term accounts with deposits being made in a later lesson.
11.a. \$268
b. $\$ 179.38$
c. $\$ 1,211.51$
d. About 20 months
e. About 22 months
f. $5.56 \%$
g. $\$ 4,545.45$
h. $x /(0.03 P)$
11. Use the simple interest formula to find the missing entries in the table. Round monetary amounts to the nearest cent.

| Interest | Principal | Rate (to the nearest hundredth of a percent) | Time |
| :---: | :---: | :---: | :---: |
| a. | \$2,000 | 3.35\% | 4 years |
| b. | \$3,500 | 4.1\% | 15 months |
| c. | \$20,100 | 5.5\% | 400 days |
| \$100 | \$700 | 8.8\% | d. |
| \$250 | \$3,000 | $4 \frac{3}{4} \%$ | e. |
| \$500 | \$3,000 | f. | 3 years |
| \$500 | g. | 4.4\% | 30 months |
| $x$ | P | 3\% | h. |

12. How much simple interest does $\$ 2,560$ earn in 17 months at a rate of $1 \frac{1}{8} \%$ ? Round to the nearest cent. $\$ 40.80$
13. How long does it take $\$ 450$ to double at a simple interest rate of $14 \%$ ? Approximately 86 months
14. How long does it take $\$ 450$ to double at a simple interest rate of $100 \%$ ? One year
15. What interest rate is needed for $\$ 9,500$ to earn $\$ 900$ in 19 months? Round to the nearest hundredth of a percent. $5.98 \%$
16. Assume $\$ 20,000$ is deposited into a savings account. Bedford Bank offers an annual rate of $1 \%$ simple interest for 5 years. Slick Bank offers a rate of $5.1 \%$ simple interest for 1 year. Which earns more interest? Slick Bank
17. Assume $\$ x$ is deposited into a savings account. Blank Bank offers an annual rate of $r \%$ for $y$ years. Thank Bank offers a rate of $r y \%$ for 1 year. Which earns more interest? Neither-they are the same.
18. A couple is opening a savings account for a newborn baby. They start with $\$ 3,450$ received in baby gifts. If no deposits or withdrawals are made, what is the balance of the account if it earns simple interest at $5 \%$ for 18 years? $\$ 6,555$
19. Ron estimates that it will cost $\$ 400,000$ to send his daughter to a private college in 18 years. He currently has $\$ 90,000$ to deposit in an account. What simple interest rate must his account have to reach a balance of $\$ 400,000$ in 18 years? Round to the nearest percent. 19\%
20. Maaz has a bank account with less than $\$ 400$ in it. His bank pays no interest on that account and charges $\$ 2$ per month for each month the account is below $\$ 500$. How much will be in Maaz's account if he makes no deposits or withdrawals after 2 years? Less than \$352
21. Zoe creates a spreadsheet to make simple interest calculations. The user inputs values for the principal, rate, and time in years in row 2 . Write each formula.
a. For A 2 to compute the interest. $=\mathrm{B} 2^{*} \mathrm{C} 2^{*} \mathrm{D} 2$
b. For B 2 to compute the principal. $=\mathrm{A} 2 /\left(\mathrm{C} 2^{*} \mathrm{D} 2\right)$
c. For C 2 to compute the interest rate. $=\mathrm{A} 2 /\left(\mathrm{B} 2^{*} \mathrm{D} 2\right)$
d. For D2 to compute time in years, given the interest, rate, and the principal. $=\mathrm{A} 2 /\left(\mathrm{B} 2^{*} \mathrm{C} 2\right)$
e. For E 2 to compute the time in months, given the time in years. $=12^{*} \mathrm{D} 2$
22. Find the missing terms indicated by variables in the arithmetic sequence shown.
$a, 30, b, 42, c, d, e \quad a=24 ; b=36 ; c=48 ; d=54 ; e=60$
