## Applications

Genius is $1 \%$ inspiration and $99 \%$ perspiration. Accordingly, a genius is often merely a talented person who has done all of his or her homework.
-Thomas Edison, inventor

1. What do you think Thomas Edison meant by the word perspiration? How do those words apply to what you've learned about businesses in this lesson? See margin.
2. Tomika owns $3 / 5$ of a law partnership. What percent of the partnership does she own? 60\%
3. Ryan owns $3 / 8$ of a florist shop worth $\$ 76,000$. What is the value of Ryan's share of the business? $\$ 28,500$
4. A corporation issues $1,200,000$ shares of stock to shareholders. How many shares must a shareholder own to have a majority of the shares? 600,001
5. Elisa owns $28 \%$ of Grudman Corp. The rest of the shares are owned equally by the remaining six shareholders. What percent of the corporation does each of the other shareholders own? $12 \%$
6. Julie and Kristen are the partners in a local sporting goods shop. They needed $\$ 51,000$ to start the business. They invested in the ratio $5: 12$, respectively.
a. How much money did each invest? Julie, $\$ 15,000$; Kristin, $\$ 36,000$
b. What percent of the business was owned by Kristin? Round to the nearest tenth of a percent. $70.6 \%$
c. If the business grows to $\$ 3,000,000$, what percent of it will Julie own? Round to the nearest tenth of a percent. $29.4 \%$
7. Joe, Thea, and Taylor invested in a partnership in the ratio 1:4:7, respectively. Years later, when the partnership was worth $\$ 1.6$ million, Thea decides to go to graduate school and sells her part of the partnership to Joe.
a. How much would Joe need to pay Thea to buy her share of the business? Round to the nearest dollar. $\$ 533,333$
b. What percent of the business will Joe own after he buys Thea's portion? Round to the nearest tenth of a percent. 41.7\%
8. Seventy-two percent of the shareholders in a service corporation are women. If the corporation is owned by 45,600 people, how many of the shareholders are women? 32,832
9. The 120 shareholders of a corporation are voting for a new board of directors. Shareholders receive one vote for each share they own. Would it be possible for one shareholder's votes to choose the new board of directors? Explain. See margin.
10. The top $x$ shareholders in a corporation each own $y$ shares of a certain stock. The corporation's ownership is represented by a total of $w$ shares of stock. Express the percent of the corporation owned by the top $x$ shareholders. $100 \frac{x y}{w}$

## TEACH <br> Fractional Parts

Throughout the applications, students will be examining fractional parts of a whole. They will be using percents primarily, and fractions less frequently.

## Percents

Because percents always compare a number to the number 100, it is easier to get an intuitive feel for a percent. For example, if a student scored 17 out of 25 on a quiz, he would likely convert it to a percent to gauge his success.

## Exercise 6

Point out to students that if the ratio is $5: 12$, then Julie owns $\frac{5}{17}$ of the business.

## Exercise 9

Yes, if one person owns more than $50 \%$ of the shares.

## Exercise 10

Students will frequently need to multiply by 100 to convert decimals to equivalent percents.

## ANSWERS

1. Edison is stressing that good ideas are not enough to achieve success. A strong work ethic is also necessary. The word "perspiration" represents the effort required.

## TEACH

As the section closes, review the important difference between a corporation and a partnershipthe concept of limited liability.

## ANSWERS

Exercise 12
Due to limited liability, the shareholders forfeit \$0 of personal property. Their stock loses value.

## Exercise 13

\$100,000 because partners are personally liable

## Exercise 15

Since they incorporated, they are personally liable for \$0. They will, however, lose their shares in the business.
11. A corporation is having a shareholders meeting to vote on a new issue. Not all shareholders are able to attend. In fact, most usually do not. The ownership of the corporation is represented by $2,351,000$ shares of stock owned by 111,273 shareholders.
a. Must all of the shareholders own more than one share of stock? No
b. If 3,411 shareholders attend the meeting, what percent of the shareholders attended the meeting? Round to the nearest percent. 3\%
c. If the shareholders who do not attend own a combined 1.8 million shares of the corporation and the shareholders are voting on a particular issue, these shareholders can vote by proxy-an absentee ballot. If 100,000 of the shareholders vote by proxy, what percent of the shareholders did not vote at all? Round to the nearest percent. $7 \%$
12. A private corporation owned by 35 shareholders is worth $\$ 1.7$ million. The corporation loses a lawsuit worth $\$ 3$ million. What is the value of any personal property of the shareholders that can be taken to pay the settlement? Explain. See margin.
13. A partnership owned equally by 13 partners is worth $\$ 1.3$ million. The partnership loses a lawsuit worth $\$ 3$ million. What is the value of any personal property each partner must forfeit to pay the settlement? Explain. See margin.
14. A sole proprietorship is worth $w$ dollars. The owner loses a lawsuit against him for $y$ dollars, where $y>w$. Express algebraically the value of the personal property the owner must forfeit to pay the settlement. $y-w$
15. Six equal partners own a local pizzeria. The partners have made a tremendous profit and bought many personal items such as cars, boats, new homes, and so on. In order to protect their personal possessions, they decide to incorporate the pizzeria, so that the six partners own shares in the corporation and have limited liability. The business is worth $\$ 675,000$. After an accident, the partners lose a lawsuit and have to pay $\$ 1.2$ million in damages. How much money will each partner personally lose to pay this lawsuit? Explain. See mary
16. Three people invest in a business. The first two invest in the ratio $2: 3$, and the third person invests twice as much as the other two combined. The total invested is $\$ 30$ million.
a. How much did the major investor contribute? $\$ 20$ million
b. Does the major investor own more than half the business? Yes
c. What fraction of the business does the major investor own? $\frac{2}{3}$
17. Ten years ago, Lisa bought a hair salon for $x$ dollars. She built up the business and it is now worth nine times what she paid for it. She decides to sell half of the business to a friend, and they become partners. Express the amount Lisa's friend must pay Lisa to buy half the business. $\frac{9 x}{2}$
18. Four people invested in a restaurant. One person invested $\$ 100,000$. Two others invested in the ratio $x: 2 x$, and the fourth person invested an amount equal to the other three investors combined.
The total investment was $\$ 1,100,000$.
a. Write an expression for the amount invested by the fourth person. 100,000
b. Write an equation that allows you to find the amount invested by each person. $2(100,000+3 x)=1,100,000$
c. How much did each person invest? $\$ 100,000 ; \$ 150,000 ; \$ 300,000 ; \$ 550,000$

